



Modeling Temporal Correlations and Dynamics in Spatiotemporal Data Systems

Xinyu Chen April 19, 2024

Outline

A quick look:

- Motivation (data, task, and models)
- Traffic data imputation with global/local trend modeling
 - $\circ\;$ Traffic flow imputation, speed field reconstruction, and network traffic state estimation
- Unsupervised pattern discovery from spatiotemporal systems
 - $\circ~$ Time-varying autoregression & tensor factorization
 - Applications to fluid flow (benchmark), sea surface temperature, USA climate, NYC taxi, international trade, and Chicago ridesharing

Motivation

• Spatiotemporal systems & data scenarios



• Challenges: Sparse data, time-varying system, multidimensional system (e.g., human mobility)

- Sequence models: Time series autoregression, LSTM, attention-based sequence models, etc.
- Machine learning problems:
 - Imputation/Interpolation: Time series models, sparse learning (e.g., matrix/tensor factorization), deep learning (e.g., generative models), etc.
 - Unsupervised pattern discovery: Dynamic mode decomposition in dynamical systems, matrix/tensor factorization, etc.
 - $\circ\;$ Prediction: Almost deep learning, but depending on scenarios

Laplacian Convolutional Representation for Traffic Time Series Imputation

2nd round review at IEEE Transactions on Knowledge and Data Engineering



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Materials:

- PDF: https://xinychen.github.io/papers/Laplacian_convolution.pdf
- GitHub: https://github.com/xinychen/transdim (1.1k+ stars)
- Blog:

https://spatiotemporal-data.github.io/posts/laplacian_convolution/
(coming soon)

Portland highway traffic data¹



- $\boldsymbol{X} \in \mathbb{R}^{N \times T}$ with N spatial locations \times T time steps
- Traffic volume/speed shows strong spatial/temporal dependencies

¹https://portal.its.pdx.edu/home

Motivation: Traffic imputation

• Global trends (e.g., long-term quasi-seasonality & daily/weekly rhythm):



• Local trends (e.g., short-term time series trends):



How to characterize both global and local trends in sparse time series?

Intuition of (circulant) Laplacian matrix



• Define Laplacian kernel:

for any time series $\boldsymbol{x} = (x_1, \dots, x_T)^\top \in \mathbb{R}^T.$

• (Laplacian) Temporal regularization:

$$\mathcal{R}_{\tau}(\boldsymbol{x}) = \frac{1}{2} \|\boldsymbol{L}\boldsymbol{x}\|_{2}^{2} = \frac{1}{2} \|\boldsymbol{\ell} \star \boldsymbol{x}\|_{2}^{2}$$

Reformulate temporal regularization with circular convolution.

Global Trend Modeling

Circulant matrix $\mathcal{C}(\boldsymbol{x})$ vs. convolution matrix $\mathcal{C}_{\tilde{\tau}}(\boldsymbol{x})$



Global Trend Modeling

Circulant matrix $\mathcal{C}(\boldsymbol{x})$ vs. convolution matrix $\mathcal{C}_{\tilde{\tau}}(\boldsymbol{x})$



- Circulant/Convolution nuclear norm minimization
 - A balance between global and local trends modeling?



ConvNNM (Liu'22, Liu & Zhang'23)
Estimating x :
$egin{array}{l} \min_{m{x}} \ \ \mathcal{C}_{ ilde{ au}}(m{x})\ _{*} \ & \ & \ & \ & \ & \ & \ & \ & \ & \ $
on data \boldsymbol{y} w/ observed index set Ω .

Laplacian Convolutional Representation (LCR)

For any partially observed time series $\boldsymbol{y} \in \mathbb{R}^T$ with observed index set Ω , LCR utilizes circulant matrix and Laplacian kernel to characterize global and local trends in time series, respectively, i.e.,

$$\min_{\boldsymbol{x}} \quad \underbrace{\|\mathcal{C}(\boldsymbol{x})\|_{*}}_{\text{global}} + \frac{\gamma}{2} \underbrace{\|\boldsymbol{\ell} \star \boldsymbol{x}\|_{2}^{2}}_{\text{local}}$$
s.t. $\|\mathcal{P}_{\Omega}(\boldsymbol{x} - \boldsymbol{y})\|_{2} \le \epsilon$



• Augmented Lagrangian function:²

$$\mathcal{L}(\boldsymbol{x}, \boldsymbol{z}, \boldsymbol{w}) = \|\mathcal{C}(\boldsymbol{x})\|_* + \frac{\gamma}{2} \|\boldsymbol{\ell} \star \boldsymbol{x}\|_2^2 + \frac{\lambda}{2} \|\boldsymbol{x} - \boldsymbol{z}\|_2^2 + \langle \boldsymbol{w}, \boldsymbol{x} - \boldsymbol{z} \rangle + \frac{\eta}{2} \|\mathcal{P}_{\Omega}(\boldsymbol{z} - \boldsymbol{y})\|_2^2$$

• The ADMM scheme:

$$\begin{cases} \boldsymbol{x} := \underset{\boldsymbol{x}}{\operatorname{arg\,min}} \mathcal{L}(\boldsymbol{x}, \boldsymbol{z}, \boldsymbol{w}) & (\text{Nuclear norm minimization}) \\ \boldsymbol{z} := \underset{\boldsymbol{z}}{\operatorname{arg\,min}} \mathcal{L}(\boldsymbol{x}, \boldsymbol{z}, \boldsymbol{w}) & (\text{Closed-form solution}) \\ \boldsymbol{w} := \boldsymbol{w} + \lambda(\boldsymbol{x} - \boldsymbol{z}) & (\text{Standard update}) \end{cases}$$

• Optimize *x*?

$$\|\mathcal{C}(\boldsymbol{x})\|_{*} = \|\mathcal{F}(\boldsymbol{x})\|_{1} \qquad \& \qquad \frac{1}{2} \|\boldsymbol{\ell} \star \boldsymbol{x}\|_{2}^{2} = \frac{1}{2T} \|\mathcal{F}(\boldsymbol{\ell}) \circ \mathcal{F}(\boldsymbol{x})\|_{2}^{2}$$

Nuclear norm minimization $\Rightarrow \ell_1$ -norm minimization with FFT in $\mathcal{O}(T \log T)$ time.

 $\overline{{}^2w\in \mathbb{R}^T}$ (Lagrange multiplier); $\langle\cdot,\cdot
angle$ (inner product).

• Optimize \boldsymbol{x} via FFT (in $\mathcal{O}(T \log T)$ time):

$$\begin{split} \boldsymbol{x} &:= \arg\min_{\boldsymbol{x}} \ \|\mathcal{C}(\boldsymbol{x})\|_{*} + \frac{\gamma}{2} \|\boldsymbol{\ell} \star \boldsymbol{x}\|_{2}^{2} + \frac{\lambda}{2} \|\boldsymbol{x} - \boldsymbol{z} + \boldsymbol{w}/\lambda\|_{2}^{2} \\ \Longrightarrow \hat{\boldsymbol{x}} &:= \arg\min_{\hat{\boldsymbol{x}}} \ \|\hat{\boldsymbol{x}}\|_{1} + \frac{\gamma}{2T} \|\hat{\boldsymbol{\ell}} \circ \hat{\boldsymbol{x}}\|_{2}^{2} + \frac{\lambda}{2T} \|\hat{\boldsymbol{x}} - \hat{\boldsymbol{z}} + \hat{\boldsymbol{w}}/\lambda\|_{2}^{2} \end{split}$$

where we introduce $\{\hat{\ell}, \hat{x}, \hat{z}, \hat{w}\} \triangleq \mathcal{F}\{\ell, x, z, w\}$ (i.e., FFT).

ℓ_1 -norm Minimization in Complex Space (Liu & Zhang'23)

For any optimization problem in the form of ℓ_1 -norm minimization in complex space:

$$\min_{\hat{\bm{x}}} \|\hat{\bm{x}}\|_1 + \frac{\delta}{2} \|\hat{\bm{x}} - \hat{\bm{h}}\|_2^2$$

with complex-valued $\hat{x}, \hat{h} \in \mathbb{C}^T$ and weight parameter δ , element-wise, the solution is given by

$$\hat{x}_t := \frac{h_t}{|\hat{h}_t|} \cdot \max\{0, |\hat{h}_t| - 1/\delta\}, t = 1, \dots, T.$$

Empirical time complexity

On the synthetic data $\boldsymbol{y} \in \mathbb{R}^T$ with $T \in \{2^{10}, 2^{11}, \dots, 2^{20}\}$

- Ours: LCR
 - An FFT implementation in $\mathcal{O}(T \log T)$
 - $\circ~$ The logarithmic factor $\log T$ makes the FFT highly efficient
- Baseline: ConvNNM (Liu'22, Liu & Zhang'23)
 - $\circ~$ Convolution matrix $\mathcal{C}_{\tilde{\tau}}(\boldsymbol{y}) \in \mathbb{R}^{T \times \tilde{\tau}}$ with kernel size $\tilde{\tau} = 2^4$
 - Singular value thresholding in $\mathcal{O}(ilde{ au}^2 T)$



Experiments



- How to utilize the global trends of traffic time series?
- How to produce local consistency of traffic data?

Experiments



CircNNM:

 $\min_{\boldsymbol{x}} \|\mathcal{C}(\boldsymbol{x})\|_*$ s.t. $\|\mathcal{P}_{\Omega}(\boldsymbol{x}-\boldsymbol{y})\|_{2} \leq \epsilon$

LCR:

$$\min_{\boldsymbol{x}} \|\mathcal{C}(\boldsymbol{x})\|_* + \frac{\gamma}{2} \|\boldsymbol{\ell} \star \boldsymbol{x}\|_2^2$$

s.t. $\|\mathcal{P}_{\Omega}(\boldsymbol{x} - \boldsymbol{y})\|_2 \leq \epsilon$

• The start data points and end data points are connected?



• Flipping operation on $\boldsymbol{x} \in \mathbb{R}^5$:

$$\boldsymbol{x}_{\text{new}} = \begin{bmatrix} \boldsymbol{x} \\ \boldsymbol{J} \boldsymbol{x} \end{bmatrix} = \underbrace{(\underbrace{\boldsymbol{x}_1, \boldsymbol{x}_2, \boldsymbol{x}_3, \boldsymbol{x}_4, \boldsymbol{x}_5}_{\text{original time series}}, \underbrace{\underbrace{\boldsymbol{x}_5, \boldsymbol{x}_4, \boldsymbol{x}_3, \boldsymbol{x}_2, \boldsymbol{x}_1}_{\text{flipped time series}})^\top \in \mathbb{R}^{10}$$

where $\boldsymbol{J} \in \mathbb{R}^{5 \times 5}$ is the exchange matrix.

• Potential applications: Passenger flow prediction with strong global/local trends

Experiments

Speed field reconstruction³

• Flipping operation on a matrix:



• Flipping operation on a speed field of vehicular traffic flow:



³Highway Drone (HighD) dataset at https://www.highd-dataset.com/

Experiments

Speed field reconstruction⁴

- Scenario: Mask trajectories of 70% vehicles
- LCR-2D on partially observed $\boldsymbol{Y} \in \mathbb{R}^{N \times T}$:





⁴Highway Drone (HighD) dataset at https://www.highd-dataset.com/

Contributions



Vision & Insight



Highlights:

- Rethinking the importance of local trend modeling in traffic data imputation tasks.
- Finding a unified global and local trend modeling framework whose optimization can be efficiently solved by FFT:

$$\min_{\boldsymbol{x}} \quad \underbrace{\|\mathcal{C}(\boldsymbol{x})\|_{*}}_{\text{global}} + \frac{\gamma}{2} \underbrace{\|\boldsymbol{\ell} \star \boldsymbol{x}\|_{2}^{2}}_{\text{local}}$$
s. t. $\|\mathcal{P}_{\Omega}(\boldsymbol{x} - \boldsymbol{y})\|_{2} \le \epsilon$

• Uber (hourly) movement speed data⁵



NYC movement



Seattle movement

- {road segment, time slot (hour), average speed}
- Computing hourly speed: Road segments have 5+ unique trips.
- Estimating network-wide traffic states for traffic planning & management. (Data/model biases/fairness concerns for imputation, interpolation, and prediction.)

⁵https://movement.uber.com/ (not available now)

Discovering Dynamic Patterns from Spatiotemporal Data with Time-Varying Low-Rank Autoregression

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Materials:

- PDF: https://xinychen.github.io/papers/time_varying_model.pdf
- GitHub: https://github.com/xinychen/vars
- Blog: https://spatiotemporal-data.github.io/posts/time_varying_model

• How to characterize dynamical systems?



• How to characterize dynamical systems?





Time-varying autoregression

• On spatiotemporal systems $\boldsymbol{Y} \in \mathbb{R}^{N imes T}$:

$$\underbrace{\boldsymbol{y}_{t+1} = \boldsymbol{A}\boldsymbol{y}_t + \boldsymbol{\epsilon}_t}_{\text{time-invariant}} \quad \text{v.s.} \quad \underbrace{\boldsymbol{y}_{t+1} = \boldsymbol{A}_t \boldsymbol{y}_t + \boldsymbol{\epsilon}_t}_{\text{time-varying}}$$

• How to discover spatial/temporal modes (patterns) from the tensor $\mathcal{A} \triangleq \{A_t\}_{t \in [T-1]}$?





• Tensor factorization⁶:

$$\mathbf{A} = \underbrace{\mathbf{\mathcal{G}}_{\times_1} \mathbf{W}_{\times_2} \mathbf{V}_{\times_3} \mathbf{X}}_{\text{Tucker decomposition}}$$

$$\widehat{\mathbf{A}}_t = \mathbf{\mathcal{G}}_{\times_1} \underbrace{\mathbf{W}}_{\text{spatial modes}} \times_2 \mathbf{V}_{\times_3} \underbrace{\mathbf{x}_t^{\mathsf{T}}}_{\text{temporal modes}}$$

• (Ours) Time-varying low-rank autoregression:

$$\min_{\boldsymbol{\mathcal{G}}, \boldsymbol{W}, \boldsymbol{V}, \boldsymbol{X}} \ \frac{1}{2} \sum_{t \in [T-1]} \left\| \boldsymbol{y}_{t+1} - (\boldsymbol{\mathcal{G}} \times_1 \boldsymbol{W} \times_2 \boldsymbol{V} \times_3 \boldsymbol{x}_t^\top) \boldsymbol{y}_t \right\|_2^2$$

• Alternating minimization: $\boldsymbol{\mathcal{G}}$ (LS) \rightarrow \boldsymbol{W} (LS) \rightarrow \boldsymbol{V} (CG) \rightarrow \boldsymbol{x}_t (LS)

 $^{^{6}\}times_{k},\,\forall k$ is the mode-k product between tensor and matrix/vector.

Fluid Flow

• Multiresolution fluid flow dataset (the first 50 snapshots + 50 snapshots randomly selected from the last 100 snapshots)



• Produce interpretable patterns and identify the system of different frequencies.

• Sea surface temperature (SST) dataset



• Identify two strongest El Nino events (on 1997-98 & 2014-16).

- Data⁷: 5,380 stations & 12 years with the day resolution
- Spatial distribution of mean temperature



• Time series of mean temperatures



⁷https://daac.ornl.gov/DAYMET

USA Temperature



Spatial patterns in \boldsymbol{W}



Temporal patterns over 12 years



Temporal patterns over 2 years

NYC Taxi Data

• NYC taxi dataset (pickup)



Dynamic Autoregressive Tensor Factorization for Pattern Discovery of Spatiotemporal Systems International Trade & Ridesharing Mobility

How to characterize dynamical systems?







Time-varying autoregression

• On spatiotemporal systems $\boldsymbol{Y} \in \mathbb{R}^{N \times T}$:

$$\underbrace{\boldsymbol{y}_{t+1} = \boldsymbol{A}\boldsymbol{y}_t + \boldsymbol{\epsilon}_t}_{\text{time-invariant}} \quad \text{v.s.} \quad \underbrace{\boldsymbol{y}_{t+1} = \boldsymbol{A}_t \boldsymbol{y}_t + \boldsymbol{\epsilon}_t}_{\text{time-varying}}$$

• How to discover spatial/temporal modes (patterns) from the tensor $\mathcal{A} \triangleq {\{A_t\}_{t \in [T-1]}}$?



DATF

• Tensor factorization⁸:



• (Ours) Dynamic autoregressive tensor factorization (DATF):

$$\min_{\boldsymbol{\mathcal{G}}, \boldsymbol{W}, \boldsymbol{V}, \boldsymbol{X}} \frac{1}{2} \sum_{t \in [T-1]} \left\| \boldsymbol{y}_{t+1} - (\boldsymbol{\mathcal{G}} \times_1 \boldsymbol{W} \times_2 \boldsymbol{V} \times_3 \boldsymbol{x}_t^{\mathsf{T}}) \boldsymbol{y}_t \right\|_2^2$$

s.t.
$$\underbrace{\boldsymbol{W}^{\mathsf{T}} \boldsymbol{W} = \boldsymbol{I}_R}_{\text{orthogonal spatial modes}}$$

• Solution: \mathcal{G} (LS) \rightarrow W (OPP) \rightarrow V (CG) \rightarrow x_t (LS)

 $^8 \times_k$, $\forall k$ is the mode-k product between tensor and matrix/vector.

• Orthogonal Procrustes problem: For any $Q \in \mathbb{R}^{m \times r}$, $m \ge r$, the solution to

$$\min_{F} \|F - Q\|_{F}^{2}$$

s.t.
$$\underbrace{F^{\top}F = I_{r}}_{\text{orthogonal}}$$

is

$$F := UV^{\top}$$

where

$$\underline{Q} = U \Sigma V^{ op}$$
singular value decomposition

• Equivalent form:

$$\begin{split} \|\boldsymbol{F} - \boldsymbol{Q}\|_{F}^{2} &= \operatorname{tr}(\boldsymbol{F}^{\top}\boldsymbol{F} - \boldsymbol{F}^{\top}\boldsymbol{Q} - \boldsymbol{Q}^{\top}\boldsymbol{F} + \underbrace{\boldsymbol{Q}^{\top}\boldsymbol{Q}}_{\operatorname{const.}}) = -2\operatorname{tr}(\boldsymbol{F}^{\top}\boldsymbol{Q}) + \operatorname{const.} \\ \Longrightarrow \boldsymbol{F} &=: \operatorname*{arg\,min}_{F^{\top}F = I_{r}} \|\boldsymbol{F} - \boldsymbol{Q}\|_{F}^{2} = \operatorname*{arg\,max}_{F^{\top}F = I_{r}} \operatorname{tr}(\boldsymbol{F}^{\top}\boldsymbol{Q}) \end{split}$$





- Multi-resolution fluid flow dataset (the first 50 snapshots + 50 snapshots randomly selected from the last 100 snapshots)
 - Produce interpretable patterns: Low-frequency modes (dominant patterns) & high-frequency modes (e.g., secondary patterns, outliers)
 - $\circ~$ Identify the system of different frequencies (i.e., at t=50)



- Import/Export merchandise trade values (annual)⁹ (215 countries/regions & period of 2000-2022)
 - Total merchadise trade values
 - \circ Represent import/export trade data as a 215-by-23 matrix



Imports from 2000 to 2022

Exports from 2000 to 2022

⁹The dataset is available at https://stats.wto.org.



• Three-dimensional trade (Economy, Product, Year)



• On spatiotemporal systems $\boldsymbol{\mathcal{Y}} \in \mathbb{R}^{M imes N imes T}$:

$$\underbrace{\boldsymbol{y}_{n,t+1} = \boldsymbol{A}_{n,t} \boldsymbol{y}_{n,t} + \boldsymbol{\epsilon}_{n,t}}_{\text{time-varying & product-varying}}$$

• Optimization problem of DATF:

$$\min_{\boldsymbol{\mathcal{G}}, \boldsymbol{W}, \boldsymbol{U}, \boldsymbol{V}, \boldsymbol{X}} \quad \frac{1}{2} \sum_{n \in [N]} \sum_{t \in [T-1]} \left\| \boldsymbol{y}_{n,t+1} - (\boldsymbol{\mathcal{G}} \times_1 \boldsymbol{W} \times_2 \boldsymbol{U} \times_3 \boldsymbol{V} \times_4 \boldsymbol{x}_t^{\mathsf{T}}) \boldsymbol{y}_{n,t} \right\|_2^2$$
s.t.
$$\underbrace{\boldsymbol{W}^{\mathsf{T}} \boldsymbol{W} = \boldsymbol{I}_R}_{\text{orthogonal country patterns}}$$

• On 17 merchandise types



- · Classify import/export merchandise according to product patterns
- Basic principle:

Import: What we buy? (demand) vs. Export: What we sell? (supply)

• On 17 merchandise types



- Classify import/export merchandise according to product patterns
- Basic principle:

Import: What we buy? (demand) vs. Export: What we sell? (supply)

Product Patterns

• On 17 merchandise types



- Classify import/export merchandise according to product patterns
- Basic principle:

Import: What we buy? (demand) vs. Export: What we sell? (supply)

• Origin-Destination (OD) matrices



• On spatiotemporal systems $\boldsymbol{\mathcal{Y}} \in \mathbb{R}^{M imes N imes T}$:

$$\underbrace{ \boldsymbol{y}_{n,t+1} = \boldsymbol{A}_{n,t} \boldsymbol{y}_{n,t} + \boldsymbol{\epsilon}_{n,t} }_{\text{time-varying \& destination-varying}}$$

• Optimization problem of DATF:

$$\min_{\boldsymbol{\mathcal{G}}, \boldsymbol{W}, \boldsymbol{U}, \boldsymbol{V}, \boldsymbol{X}} \quad \frac{1}{2} \sum_{n \in [N]} \sum_{t \in [T-1]} \left\| \boldsymbol{y}_{n,t+1} - (\boldsymbol{\mathcal{G}} \times_1 \boldsymbol{W} \times_2 \boldsymbol{U} \times_3 \boldsymbol{V} \times_4 \boldsymbol{x}_t^{\mathsf{T}}) \boldsymbol{y}_{n,t} \right\|_2^2$$
s.t.
$$\underbrace{\boldsymbol{W}^{\mathsf{T}} \boldsymbol{W} = \boldsymbol{I}_R}_{\text{orthogonal origin patterns}}$$

Human Mobility

٠ Chicago taxi/ridesharing data

Matching Taxi Trips with Community Areas

There are three basic steps to follow for processing taxi trip data:

- Download taxi trips in 2022 in the .ow format. e.g., Taxi, Trips 2022.org.
- · Use the pender package in Python to process the raw trip data. Match trip pickup/dropoff locations with boundaries of the community area.

data - pl.cond_cov("tast_trips_-_itt22.cov")

For each taxi trip, one can select some important information:

- . Trip Start Timestance When the trip started, rounded to the nearest 15 minutes.
- . True Seconds: Time of the trip in seconds.
- . Trip Niles: Distance of the trip in miles.
- · Plotop Computity Area: The Community Area where the trip began. This column will be blank for locations ourside Chicago.
- Dranoff, Community, Area: The Community Area where the trip ended. This column will be blank for locations outside Chicago.

dd('Trip Start Timestamp') - dataj'Trip Start Timestamp')
df['Trip Records'] - dats['Trip Records']
df('Trip Hiles') - dets('Trip Hiles')
df('Dielop Community Area') - data('Pickup Community Area')
df('brupoff Commaxity Area') - data('brupoff Commanity Area')

Figure 2 shows taxi pickup and dropoff trips (2022) on 77 community areas in the City of Chicago. Note that the average trip duration is 1207.75 seconds and the average trip distance is 8.18 miles



Figure 2. Taxi pickup and dropoff trips (2022) in the City of Chicago, USA. There are 4,763,961 remaining trips after the data processing.

For comparison, Figure 3 shows taxi pickup and dropoff trips (2019) on 77 community areas in the City of Chicago. Note that the average trip duration is 915.62 seconds and the average trip distance is 3.93 miles



Figure 3. Tasi pickup and dropoff trips (2019) in the City of Chicago, USA. There are 12.484.572 remaining trips after the data processing. See the data processing codes.



Figure 6. Average travel time and speed from area 32 (i.e., Downtown) to area 76 (i.e., Aimort) in both 2019 and 2022



s1 = df2.groupby(['host'])] Trip Seconds').std().values / 31

Source: https://spatiotemporal-data.github.io/Chicago-mobility/taxi-data

• Ridesharing: 96,642,881 trips in 2019 vs. 57,290,954 trips in 2022



• Ridesharing: 96,642,881 trips in 2019 vs. 57,290,954 trips in 2022



Human Mobility

- Ridesharing trip data: 77 origins \times 77 destinations \times 168 hours
- Our model Identifies the changes in pickup zones before and after COVID-19



Conclusion

- Discovering spatial/temporal patterns from 2D and 3D spatiotemporal systems with unsupervised learning:
 - Time-varying system assumption
 - Tensor factorization formula



- Discovering spatial/temporal patterns from 2D and 3D spatiotemporal systems with unsupervised learning:
 - Time-varying system assumption
 - Tensor factorization formula







Thanks for your attention!

Any Questions?

Slides: https://xinychen.github.io/slides/temporal_modeling.pdf

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